

GITAM (Deemed to be University)
[MATH2361]
GST/GSS/GSB/GSHS. Degree Examination

IV Semester

PROBABILITY AND STATISTICS

(Effective from the admitted batch 2021-22)

Time: 2 Hours

Max. Marks: 30

Instructions: All parts of the unit must be answered in one place only.

Section-A

1. **Answer all Questions:** **(5×1=5)**

- What is the probability for a non-leap year to have 52 Mondays and 53 Sundays?
- If X is a random variable and $E(X) = 2$. Find the value of $E(2x + 4)$.
- Write the normal equations by the method of least squares to fit a straight line to the given data.
- Among 900 peoples in a state 90 are found to be chapatti eaters. Construct 99% confidence interval for the population.
- Write any two applications of F – distribution.

Section-B

Answer the following: **(5×5=25)**

UNIT-I

2. Calculate the mean and mode of the following data:

| | | | | | | | |
|-----------------|-------|-------|-------|-------|-------|-------|-------|
| Marks | 20-30 | 30-40 | 40-50 | 50-60 | 60-70 | 70-80 | 80-90 |
| No. of students | 6 | 5 | 8 | 15 | 7 | 6 | 3 |

OR

3. In a bolt factory machines A, B, C manufacture 20%,30% and 50% of the total of their output and 6%,3% and 2% are defective. A bolt is drawn at random and found to be defective. Find the probabilities that it is manufactured from (i) Machine A (ii) Machine B (iii) Machine C

UNIT-II

4. For the following probability distribution.

| | | | |
|------|---------------|---------------|---------------|
| x | 3 | 6 | 9 |
| P(x) | $\frac{1}{6}$ | $\frac{1}{2}$ | $\frac{1}{3}$ |

Find (i) $E(X)$ (ii) $E(x^2)$ (iii) $E[(2X+1)^2]$.

OR

5. A continuous random variable X has the distribution function.

$$F(X) = \begin{cases} 0, & \text{if } x \leq 1 \\ k(x-1)^5, & \text{if } 1 \leq x \leq 4 \\ 1, & \text{if } x > 4 \end{cases}$$

Determine, (i) $f(x)$ (ii) k (iii) Mean.

UNIT-III

6. Find rank correlation coefficient for the following data.

| | | | | | | | | | | |
|---|----|----|----|----|----|----|----|----|----|----|
| x | 68 | 64 | 75 | 50 | 64 | 80 | 75 | 40 | 55 | 64 |
| y | 62 | 58 | 68 | 45 | 81 | 60 | 68 | 48 | 50 | 70 |

OR

7. Find the means of X and Y from the regression equations $X = 2Y+3$, $4Y = X+6$ and also find the correlation coefficient.

UNIT-IV

8. Write down the general procedure for testing of hypothesis.

OR

9. A sample of 500 items is taken from a population whose standard deviation is 20. The mean of the sample is 50. Test whether the sample has come from a population with mean 48.

UNIT-V

10. The heights of **10** males of a given locality are found to be **70, 67, 62, 68, 61, 68, 70, 64, 64, 66** inches. Is it reasonable to believe that the average height is greater than **64** inches? Test at **5%** significance level. (t table value is 1.833).

OR

11. A group of boys and girls were given an intelligence test. The mean score, S. Ps and numbers in each group are as follows:

| | Boys | Girls |
|-------------|------|-------|
| Mean | 107 | 112 |
| S.D | 10 | 8 |
| Sample size | 16 | 14 |

Is the mean score of boy's significant different from that of girls at 5% level of significance? (t table value is 1.701).